

# Origin of the plateau in the temperature dependence of the normalized magnetization relaxation rate in disordered high-temperature superconductors

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The temperature  $T$  dependence of the normalized magnetization relaxation rate  $S$  in optimally doped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  films with the external dc magnetic field  $H$  oriented along the  $c$  axis exhibits the well-known plateau in the intermediate  $T$  range, associated with the presence of elastic (collective) vortex creep. The disappearance of the  $S(T)$  plateau in the high- $H$  domain ( $H \geq 20$  kOe) is not completely understood. We show that in the case of high-temperature superconductors with significant quenched disorder the  $S(T)$  plateau is directly related to a crossover in the vortex-creep process generated by the macroscopic currents induced in the sample. In dc magnetization measurements the creep-crossover temperature decreases rapidly with increasing  $H$ , reaching the low- $T$  region where the magnetization decay is dominated by micro flux jumps. Consequently, at high  $H$  no well-defined elastic-creep domain is present and the  $S(T)$  plateau disappears.

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The relaxation of the irreversible magnetization of high-temperature superconductors (HTSs) remains an essential tool for the investigation of vortex dynamics and the vortex phase diagram. In order to reduce the intrinsic ambiguity of flux-creep measurements,<sup>1,2</sup> many magnetization relaxation studies have focused on the analysis of the normalized magnetization relaxation rate. At low  $T$ , where the relaxation is weak, one usually determines a normalized magnetization relaxation rate averaged over a fixed relaxation-time window,  $S = -\Delta \ln(|M|) / \Delta \ln(t)$ , where  $M$  is the irreversible magnetization (proportional to the current density  $J$  of the macroscopic currents induced in the sample) and  $t$  is the relaxation time.

In the case of HTSs with relevant random quenched disorder, the  $S(T)$  variation at relatively low  $H$  exhibits three distinct regions.<sup>2-9</sup> At high  $T$ ,  $S(T)$  increases with increasing  $T$ . At intermediate  $T$  values a plateau in  $S(T)$  develops, whereas at low  $T$  a slight decrease in  $S$  with decreasing  $T$  appears. The rapid  $S(T)$  increase in the high- $T$  region is commonly attributed to thermal fluctuations, whereas the  $S(T)$  behavior at low  $T$  is associated with quantum vortex creep<sup>10</sup> or with a crossover toward an exponential time dependence of the irreversible magnetization.<sup>11</sup> The apparent universality of  $S$  in the plateau region (with values clustered around  $S \sim 10^{-2}$ ) was explained in Ref. 3 by assuming the existence of an elastic vortex glass,<sup>12</sup> with strongly nonlinear current-voltage characteristics. It was shown<sup>3</sup> that the  $S$  universality comes from the fact that in the elastic vortex-glass domain  $S$  depends on the collective (elastic) creep exponent<sup>13</sup> and only logarithmically on time parameters (which do not change very much with the system and experiment). When the dis-

order degree is weak, the above interpretation remains essentially the same, owing to the well-established collective pinning behavior in the Bragg glass domain at low  $H$ .<sup>14</sup>

For disordered HTSs, when the  $S(T)$  plateau is associated with the existence of an elastic vortex glass a question which arises is related to the disappearance of the  $S(T)$  plateau at high  $H$ . In the case of optimally doped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  (Y-123) films, for example, the elastic vortex-glass transition temperature reported from the scaling of current-voltage characteristics remains above 70 K for  $H$  as high as 100 kOe,<sup>15</sup> whereas the plateau disappears above a significantly lower  $H$ .<sup>7</sup>

In this work, we address the above issue through a detailed analysis of magnetization relaxation in high-quality Y-123 films. It is shown that the appearance of the plateau in  $S(T)$  is directly related to a crossover in the vortex-creep process generated by the macroscopic currents induced in the sample during magnetization measurements: plastic creep at high  $T$  (low  $J$ ) and elastic creep at intermediate  $T$  ( $J$ ). The  $S(T)$  plateau corresponds to the elastic-creep regime, in agreement with Ref. 3. However, in the case of dc magnetization measurements the creep-crossover temperature decreases strongly with increasing  $H$ , reaching the low- $T$  domain where the magnetization decay is highly influenced by the occurrence of micro flux jumps. At high  $H$  no well-defined elastic-creep domain is thus present and the  $S(T)$  plateau disappears.

We investigated the magnetization relaxation for disk-shaped (2.5 mm in diameter) optimally doped Y-123 films ( $\sim 250$  nm thick) prepared by high-pressure dc sputtering onto (001)-oriented  $\text{SrTiO}_3$  substrates. The inductively mea-

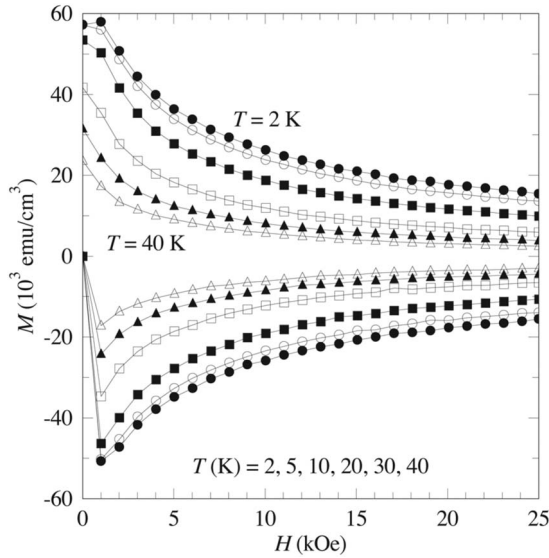


FIG. 1. Characteristic dc magnetization curves  $M(H)$  of disk-shaped optimally doped Y-123 films ( $T_c \sim 91.5$  K) for  $T$  between 2 and 40 K. One can see a limitation of  $M$  at low  $T$ .

sured critical temperature  $T_c$  is around 91.5 K for  $H=0$ , and the transition width is of the order of 0.3 K. The dc magnetization  $M$  was measured using a commercial Quantum Design magnetic property measurement system (MPMS), with  $H$  oriented along the  $c$  axis and always applied in zero-field-cooling conditions. In the considered  $(H, T)$  domain  $M$  was identified with the irreversible magnetization. The relaxation time  $t$  was taken to be zero when magnet charging was finished, and the first data point was registered at  $t_1 \sim 100$  s. The remnant state was created by applying a magnetic field  $H=10$  kOe at  $T > T_c$ , then the desired  $T < T_c$  was stabilized, and finally  $H$  was decreased to zero. The  $H$  sweeping rate in our measurements was of  $\sim 100$  Oe/s.

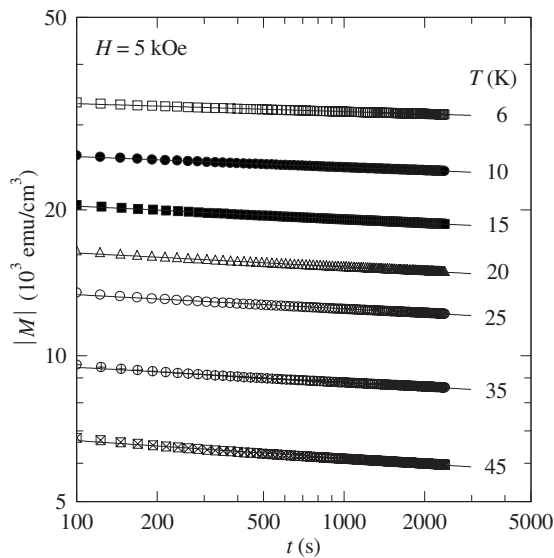


FIG. 2. Characteristic magnetization relaxation curves  $M(t)$  in double-logarithmic scales for  $H=5$  kOe and several  $T$  values well below  $T_c$ .

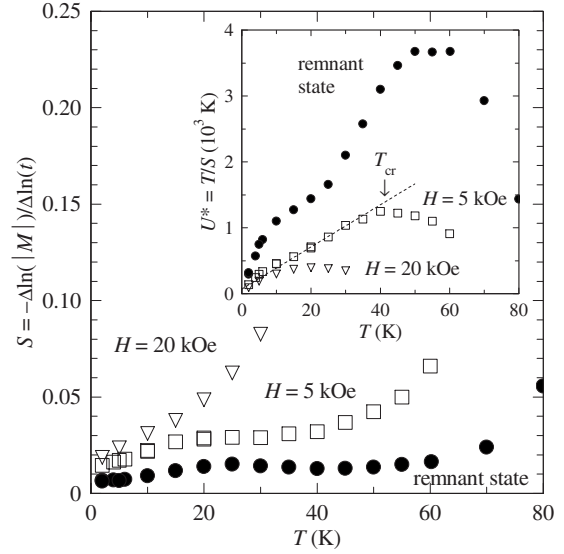


FIG. 3. Temperature variation in the normalized magnetization relaxation rate  $S = -\Delta \ln(|M|) / \Delta \ln(t)$  averaged over the relaxation-time window from Fig. 2. At low  $H$  (5 kOe and remnant state) the  $S(T)$  plateau develops above  $\sim 20$  K, but it disappears for  $H = 20$  kOe. The inset illustrates the corresponding normalized vortex-creep activation energy  $U^*(T) = T/S$ , showing a maximum at the crossover temperature  $T_{cr}$  (indicated by an arrow). The  $T$  interval for the  $S(T)$  plateau is located just below the crossover temperature  $T_{cr}$ . The linear  $U^*(T)$  variation in the plateau region has a small intercept  $U^*(0)$ . The linear fit for  $H=5$  kOe (dashed line) leads to  $U^*(0) = 70 \pm 30$  K.

Figure 1 illustrates the dc magnetization curves  $M(H)$  for  $T$  between 2 and 40 K. One can see the “limitation” of  $M$  at low  $T$ , which is attributed to the presence of micro flux jumps, as will be discussed below. Characteristic magnetization relaxation curves  $M(t)$  in double-logarithmic scales are presented in Fig. 2, and we determined the normalized magnetization relaxation rate  $S$  averaged over the (fixed) relaxation-time window  $t_w$  (100–2500 s) and the related normalized vortex-creep activation energy  $U^* = -T\Delta \ln(t) / \Delta \ln(|M|) = T/S$ .

The  $S(T)$  variation for  $H=5$  and 20 kOe and for the remnant state is plotted in the main panel of Fig. 3, whereas the corresponding  $U^*(T)$  is shown in the inset. For the remnant state and  $H=5$  kOe the  $S(T)$  plateau develops above  $\sim 20$  K. The  $T$  domain for the  $S(T)$  plateau shrinks with increasing  $H$  and the plateau disappears for  $H=20$  kOe. The  $T$  interval for the  $S(T)$  plateau is located just below the crossover temperature  $T_{cr}$  where  $U^*(T)$  exhibits a maximum. The linear  $U^*(T)$  in the plateau region has a small intercept  $U^*(0)$ .

The discussion of the results from Fig. 3 first requires the precise meaning of  $U^*$ , which is sometimes called “the effective pinning energy.” While  $U^*$  cannot actually be identified with the effective pinning barrier, this is very useful for detecting changes in the vortex-creep process. Following Ref. 16, the actual vortex-creep activation energy  $U$  can be written as

$$U(T, H, J) = (U_c/p)[(J_c/J)^p - 1], \quad (1)$$

where  $U_c$  is a characteristic pinning energy, whereas exponent  $p$  is identified with the (positive) collective pinning exponent  $\mu$  in the case of elastic (collective) vortex creep,<sup>13</sup> and  $p < 0$  for plastic creep. With Eq. (1) and  $J \propto |M|$  one can derive  $U^*(J)$  using the general creep relation<sup>17</sup>  $U = T \ln(t/t_0)$ , where  $t_0$  is a macroscopic time scale for creep<sup>1</sup> or the microscopic vortex hopping “attempt” time.<sup>3</sup> For the elastic-creep domain one obtains

$$U^*(J) = U_{ce}(J_c/J)^\mu, \quad (2)$$

where  $U_{ce}$  is the characteristic pinning energy for elastic creep. In the plastic creep regime  $U^*$  has an opposite variation with  $J$ ,

$$U^*(J) = U_{cp}(J_c/J)^p, \quad (3)$$

where  $U_{cp}$  is the characteristic pinning energy for plastic creep. With a fixed  $t_w$  and  $T$  well below  $T_c$ , the above equations lead to

$$U^* \approx U_{ce} + \mu T \ln(t_w/t_0) \quad (4)$$

for elastic creep and

$$U^* \approx U_{cp} - |p|T \ln(t_w/t_0) \quad (5)$$

in the case of plastic creep. (For simplicity, we have considered the same  $t_0$  for elastic creep and plastic creep.) The maximum in  $U^*(T)$  appearing in the inset of Fig. 3 indicates a crossover elastic creep at low  $T$ -plastic creep at high  $T$ , and, in the approximation  $t_0 = \text{const}$ , Eqs. (4) and (5) lead to a creep-crossover temperature  $T_{cr} \approx (U_{cp} - U_{ce})/[(\mu + |p|)\ln(t_w/t_0)]$ .

Since for  $H \geq 5$  kOe the observed  $T_{cr}$  is much lower than  $T_c$ , the  $U^*(T)$  decrease above  $T_{cr}$  cannot be primarily attributed to thermal fluctuations. It was shown in Ref. 18 that the creep crossover in dc magnetization measurements [leading to the nonmonotonic  $U^*(T)$  from the inset of Fig. 3] is in fact caused by the macroscopic currents induced in the sample  $J(T, t)$ . At least for  $T$  well below  $T_c$ , the main role of the thermal energy is to change the probed  $J$  domain. This is due to a different overall relaxation in the interval between the moment when magnet charging was finished ( $t \approx 0$ ) and the time  $t_1$  at which the first data point is taken. When  $T$  decreases  $J$  increases toward  $J_c$ , and below a certain  $T_{cr}$  the effective pinning energy becomes lower than the elastic energy  $E_{el}$  in the vortex system. In this situation the creep is entirely elastic since some dislocations may heal<sup>19</sup> and the others will be collectively pinned<sup>20</sup> at such high drives. Simple arguments<sup>21</sup> (based on the dynamic energy balance relation<sup>18</sup>  $U \propto E_{el} \propto H^{-1/2}$ ) lead to  $T_{cr}(H) \propto H^{-1/2}$ . With increasing  $T$  above  $T_{cr}$  the probed  $J$  interval is shifted down relative to  $J_c$ , and Eq. (3) indicates a decrease (increase) in  $U^*(S)$ . When this combines with the effect of thermal fluctuations at high  $T$ , a rapid  $S(T)$  increase above the  $S(T)$  plateau appears.<sup>7</sup>

Figure 4 illustrates  $U^*$  vs  $1/J$ , where  $J$  was extracted with the Bean model<sup>22</sup> from  $M(t)$  averaged over  $t_w$ . For the remnant state and  $H=5$  kOe a well-defined elastic-creep domain is present, where  $U^*(J)$  is given by Eq. (2), with widely

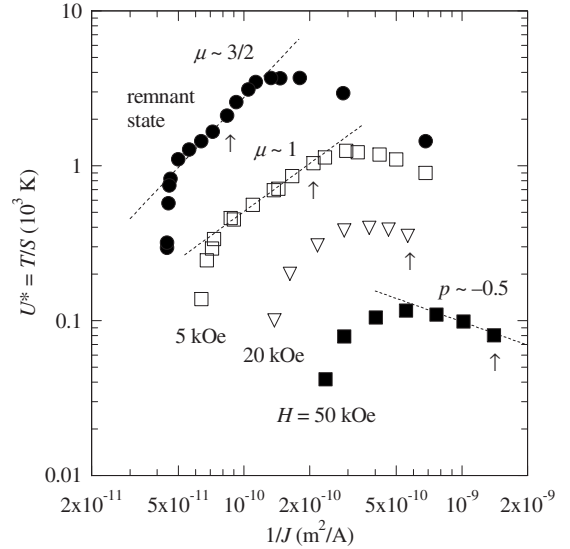


FIG. 4. The normalized vortex-creep activation energy  $U^*$  vs  $1/J$ , where  $J$  was extracted with the Bean model from  $M(t)$  averaged over the relaxation-time window from Fig. 2. For the remnant state and  $H=5$  kOe [for which the plateau in  $S(T)$  develops (Fig. 3)] a well-defined elastic-creep domain is present, where  $U^*(J)$  is given by Eq. (2), with widely accepted elastic-creep exponent  $\mu$  values for small (remnant state) and intermediate ( $H=5$  kOe) vortex bundle regimes. At  $H=20$  and 50 kOe no elastic-creep domain was observed and the  $S(T)$  plateau disappears. At high  $J$  the plastic-creep regime sets in and the plastic-creep exponent is close to the value proposed in Ref. 23 ( $p=-0.5$ ). The dashed lines represent the linear fit in the log-log plot, and the arrows indicate  $T=30$  K.

accepted  $\mu$  values.<sup>13</sup> This is in agreement with the linear  $U^*(T)$  variation from Eq. (4), where  $U_{ce} = U^*(0)$ . The intercept determined for  $H=5$  kOe in the inset of Fig. 3 indicates that  $U_{ce}$  is small, as expected for elastic creep (where the pinning centers do not accommodate vortices). Neglecting  $U_{ce}$ , Eq. (4) gives  $S(T) \approx T/U^* \approx [\mu \ln(t_w/t_0)]^{-1}$ , which is the result for the universal  $S$  in the plateau region from Ref. 3. By considering the  $S$  value in the plateau region for  $H=5$  kOe,  $\mu \sim 1$ , and  $t_w$  of the order of  $10^3$  s, one obtains  $t_0$  of the order of  $10^{-11}$  s, an accepted value for the microscopic vortex hopping attempt time.<sup>1,3</sup> For the plastic-creep domain above  $T_{cr}$ , Eq. (3) suggests a creep exponent  $p$  not far from  $-0.5$  (the value proposed in Ref. 23). Equation (5) shows that it is impossible for an  $S(T)$  plateau to appear in the plastic-creep regime, where the characteristic pinning energy  $U_{cp} > |p|T \ln(t_w/t_0)$  (for vortices better accommodated to the pinning centers at  $J \ll J_c$ ).

In the low- $T$  domain a rapid decrease in  $U^*$  with increasing  $J$  occurs (Fig. 4).  $M(t)$  cannot be related to elastic vortex creep since the resulting  $\mu$  overcomes any plausible values<sup>13</sup> and/or is strongly  $J$  dependent. Together with the  $M$  limitation at low  $T$  (Fig. 1) this suggests the occurrence of micro flux jumps, preceding the avalanches expected at even lower  $T$  and/or a higher field-sweeping rate.<sup>24</sup> For  $H=20$  kOe the creep-crossover temperature  $T_{cr}$  already reaches 20 K [the end  $T$  value for the  $S(T)$  plateau], which means that at high  $H$  the micro flux jumps set in as soon as the creep becomes elastic. In such a situation, no well-defined elastic-creep do-

main is present and the  $S(T)$  plateau disappears.

Another indication of the presence of micro flux jumps is the upturn in  $U^*(T)$  with decreasing  $T$  just below the  $S(T)$  plateau, contributing to the decrease in  $S$  (see Fig. 3 and Ref. 7). In our opinion, this upturn is caused by a (continuous) crossover between elastic-creep-dominated magnetization relaxation and micro-flux-jump-dominated magnetization decay. In the upturn region the micro flux jumps mainly appear in the  $t$  interval between  $\sim t_0$  and  $\sim t_1$ , where  $J$  is closer to  $J_c$ . The measured magnetization relaxation can still be dominated by elastic creep at  $t \geq t_1$ , but the probed  $J$  interval was already shifted to lower values, leading to a higher  $U^*$  [see Eq. (2)]. This is somehow similar to what happens in the “flux-creep annealing” process, reducing the magnetization relaxation.<sup>25</sup> In these conditions, the use of pure thermally activated creep and the same  $t_w$  become inappropriate for  $T(H)$  below (above) the end point of the  $S(T)$  plateau in the  $(H, T)$  diagram ( $T \sim 20$  K and  $H \sim 20$  kOe in the case of our

Y-123 films). The micro flux jumps seem to be responsible for the existence of a finite  $S$  in the low- $T$  limit, as an alternative to quantum vortex creep.

In summary, the existence of the plateau in  $S(T)$  for disordered HTSs appears to be directly related to a crossover in the vortex-creep process generated by the macroscopic currents induced in the sample during magnetization measurements. The  $S(T)$  plateau corresponds to the elastic-creep regime, in agreement with Ref. 3. In dc magnetization measurements the creep-crossover temperature decreases strongly with increasing  $H$ , reaching the low- $T$  domain where the magnetization decay is influenced by the occurrence of micro flux jumps. At high  $H$  no well-defined elastic-creep domain is thus present and the  $S(T)$  plateau disappears.

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- <sup>1</sup>G. Blatter, M. V. Feigel'man, V. B. Geshkenbein, A. I. Larkin, and V. M. Vinokur, *Rev. Mod. Phys.* **66**, 1125 (1994).  
<sup>2</sup>Y. Yeshurun, A. P. Malozemoff, and A. Shaulov, *Rev. Mod. Phys.* **68**, 911 (1996).  
<sup>3</sup>A. P. Malozemoff and M. P. A. Fisher, *Phys. Rev. B* **42**, 6784 (1990).  
<sup>4</sup>I. A. Campbell, L. Fruchter, and R. Cabanel, *Phys. Rev. Lett.* **64**, 1561 (1990).  
<sup>5</sup>L. Civale, A. D. Marwick, M. W. McElfresh, T. K. Worthington, A. P. Malozemoff, F. H. Holtzberg, J. R. Thompson, and M. A. Kirk, *Phys. Rev. Lett.* **65**, 1164 (1990).  
<sup>6</sup>M. Konczykowski, A. P. Malozemoff, and F. Holtzberg, *Physica C* **185-189**, 2203 (1991).  
<sup>7</sup>F. C. Klaassen, G. Doornbos, J. M. Huijbregtse, R. C. F. van der Geest, B. Dam, and R. Griessen, *Phys. Rev. B* **64**, 184523 (2001).  
<sup>8</sup>J. J. Åkerman and K. V. Rao, *Phys. Rev. B* **65**, 134525 (2002).  
<sup>9</sup>M. Peurla, H. Huhtinen, and P. Paturi, *Supercond. Sci. Technol.* **18**, 628 (2005).  
<sup>10</sup>L. Fruchter, A. P. Malozemoff, I. A. Campbell, J. Sanchez, M. Konczykowski, R. Griessen, and F. Holtzberg, *Phys. Rev. B* **43**, 8709 (1991).  
<sup>11</sup>J. R. Thompson, Y. R. Sun, and F. Holtzberg, *Phys. Rev. B* **44**, 458 (1991).  
<sup>12</sup>D. S. Fisher, M. P. A. Fisher, and D. A. Huse, *Phys. Rev. B* **43**, 130 (1991).  
<sup>13</sup>M. V. Feigel'man, V. B. Geshkenbein, A. I. Larkin, and V. M. Vinokur, *Phys. Rev. Lett.* **63**, 2303 (1989).  
<sup>14</sup>T. Giamarchi and P. Le Doussal, *Phys. Rev. B* **55**, 6577 (1997).  
<sup>15</sup>A. Sawa, H. Yamasaki, Y. Mawatari, H. Obara, M. Umeda, and S. Kosaka, *Phys. Rev. B* **58**, 2868 (1998).  
<sup>16</sup>A. P. Malozemoff, *Physica C* **185-189**, 264 (1991).  
<sup>17</sup>V. B. Geshkenbein and A. I. Larkin, *Sov. Phys. JETP* **60**, 369 (1989).  
<sup>18</sup>L. Miu, *Phys. Rev. B* **72**, 132502 (2005).  
<sup>19</sup>S. Bhattacharya and M. J. Higgins, *Phys. Rev. Lett.* **70**, 2617 (1993).  
<sup>20</sup>J. Kierfeld and V. Vinokur, *Phys. Rev. B* **61**, R14928 (2000).  
<sup>21</sup>V. Vinokur, B. Khaykovich, E. Zeldov, M. Konczykowski, R. A. Doyle, and P. Kes, *Physica C* **295**, 209 (1998).  
<sup>22</sup>C. P. Bean, *Phys. Rev. Lett.* **8**, 250 (1962).  
<sup>23</sup>Y. Abulafia, A. Shaulov, Y. Wolfus, R. Prozorov, L. Burlachkov, Y. Yeshurun, D. Majer, E. Zeldov, H. Wühl, V. B. Geshkenbein, and V. M. Vinokur, *Phys. Rev. Lett.* **77**, 1596 (1996).  
<sup>24</sup>D. V. Denisov, A. L. Rakhmanov, D. V. Shantsev, Y. M. Galperin, and T. H. Johansen, *Phys. Rev. B* **73**, 014512 (2006).  
<sup>25</sup>G. A. Levin, C. C. Almasan, D. A. Gajewski, and M. B. Maple, *Appl. Phys. Lett.* **72**, 112 (1998).